

EECS 861  
Homework 4

1. The joint distribution of  $X_1$  and  $X_2$  is  
 $f_{X_1, X_2}(x_1, x_2) = 3x_1$  for  $0 < x_1 < 1$   $0 < x_2 < x_1$  and  $f_{X_1, X_2}(x_1, x_2) = 0$  otherwise
  - a. Find the marginal pdf of  $X_1$
  - b. Find  $f_{X_2|X_1}(x_2 | x_1)$
  - c. Find  $E[X_2|X_1=1/2]$
  - d. Find  $\text{Var}[X_2|X_1=1/2]$
2.  $X$  and  $Y$  are S.I. RVs with means and standard deviations of  $\mu_X, \mu_Y, \sigma_X, \sigma_Y$ . Let  $Z = X+Y + c$ . Find the mean and variance of  $Z$ .
3. Chapter 2: Problem 2.33 a
4. Chapter 2: Problem 2.34
5. Chapter 2: Problem 2.35 a, b
6. Chapter 2: Problem 2.42
7. For the bivariate Gaussian random vector  $X$  given in problem 2.47. Find
  - a.  $E[X_1], \text{Var}[X_1], E[X_2], \text{Var}[X_2]$
  - b.  $\rho_{X_1, X_2}$
  - c.  $E[X_1 | X_2=1], \text{Var}[X_1 | X_2=1]$ ,
  - d.  $P(X_1 > 2 | X_2=1)$
8. For the bivariate Gaussian random vector  $X$  given in problem 2.47  
Find a transformation  $B, Z=BX$ , where the  $Z_1$  and  $Z_2$  are identically distributed and statistically independent with unit variance.
9.  $X$  is a RV with mean and standard deviation of  $\mu_X=0$  and  $\sigma_X$ .  $Y=aX+b$ . Find  $\rho_{XY}$
10. Plot and analyze the following data sets. Create a scatter plot and estimate  $\rho_{XY}$ , the covariance and correlation matrixes for each data set below. For estimators see <http://demonstrations.wolfram.com/CorrelationAndCovarianceOfRandomDiscreteSignal>  
What can you say about  $\rho_{XY}$  from visual examination of the scatter plot?
  - a. Data set  
[http://www.ittc.ku.edu/~frost/EECS\\_861/EECS\\_861\\_HW\\_Fall\\_2017/Homework-4-10a.csv](http://www.ittc.ku.edu/~frost/EECS_861/EECS_861_HW_Fall_2017/Homework-4-10a.csv)
  - b. Data set  
[http://www.ittc.ku.edu/~frost/EECS\\_861/EECS\\_861\\_HW\\_Fall\\_2017/Homework-4-10b.csv](http://www.ittc.ku.edu/~frost/EECS_861/EECS_861_HW_Fall_2017/Homework-4-10b.csv)
  - c. Data set  
[http://www.ittc.ku.edu/~frost/EECS\\_861/EECS\\_861\\_HW\\_Fall\\_2017/Homework-4-10c.csv](http://www.ittc.ku.edu/~frost/EECS_861/EECS_861_HW_Fall_2017/Homework-4-10c.csv)